



**MANAV RACHNA  
UNIVERSITY**

(FORMERLY MANAV RACHNA COLLEGE OF ENGINEERING  
NAAC ACCREDITED 'A' GRADE INSTITUTION)

Declared as State Private University under section 2f of the UGC act, 1956

**DEPARTMENT OF MATHEMATICS**

"T3 Examination, May 2017-18"

Semester: Second  
Subject: Discrete Mathematics  
Branch: CST  
Course Type: Core  
Time: 3 Hours  
Max.Marks: 80

Date of Exam: 15 /05/2018  
Subject Code: MAH106-T  
Session: I  
Course Nature: Hard  
Program: B.Tech  
Signature: HOD/Associate HOD: *Amik Das*

Note: All questions are compulsory from part A ( $2 \times 10 = 20$  Marks). Attempt any two questions from Part B (15 Marks each). Attempt any two Questions from Part -C (15 Marks each).

**PART -A**

- Q.1 (a) Define center of a group.  
(b) Define ring with unity.  
(c) Find the dual of the following Boolean expression  $x(\bar{y} \bar{z} + yz)$ .  
(d) Give an example of a graph which contains an Eulerian circuit that is also a Hamiltonian cycle.  
(e) Define size and order of a graph.  
(f) Define regular graph with an example.  
(g) Give the definition of cut edge of bridge of a graph.  
(h) Is there a simple graph corresponding to the degree sequence (1, 1, 2, 3).  
(i) How many vertices and edge do the graphs  $k_n$  and  $k_{m,n}$  have?  
(j) Define Isolated and pendant vertex.

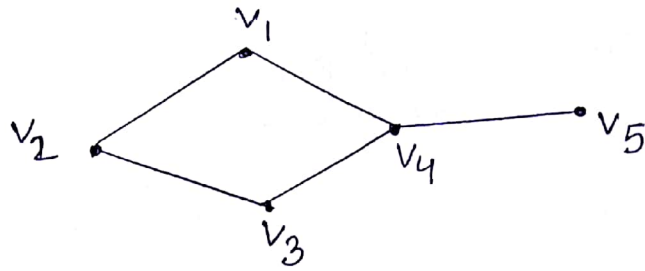
**PART - B**

- Q.2 Q.1 (a) Define a group with an example. State the axioms which a set must obey so that it may form an abelian group. Show that the set  $G = \{a + b\sqrt{2} : a, b \in \mathbb{Q}\}$  is an abelian group with respect to addition. (8)
- (b) Define subgroup. Let H be a non-empty subset of a group G, then prove that it is a sub group of G if and only if  $a * b^{-1} \in H \quad \forall a, b \in H$ . (7)
- Q.3 (a) Simplify  $Y = (P + Q)(P + \bar{Q})(\bar{P} + Q)$  using algebra method. (5)
- (b) Prove that  $a + (a \cdot b) = a$ . (3)
- (c) Define ring with zero divisor. Suppose M is a ring of all  $2 \times 2$  matrices with their elements as integer, the addition and multiplication of matrices being the two ring compositions. Then show that M is a ring with zero divisor. (7)
- Q.4 (a) Define Boolean algebra. Write down the axioms of Boolean algebra. Simplify (8)
- $Y = \sum m(0, 1, 4, 5, 6, 8, 9, 12, 13, 14)$  (7)
- (b) State and prove De' Morgan's Law in Boolean algebra.

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**PART - C**

Q.5 (i) Define subgraph of a graph. Construct two edge deleted subgraph and two vertex deleted subgraphs of a graph shown below. (5)



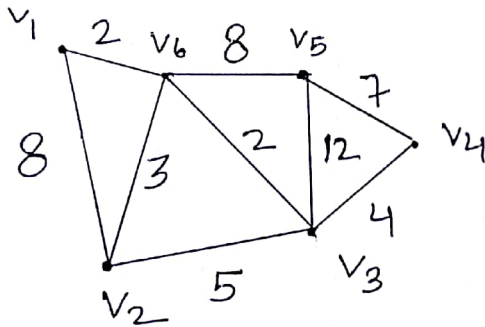
(ii) Define planar graph. Show that  $K_5$  is non-planar. (5)

(iii) Define degree of an undirected graph. A graph G has 21 edges, 3 vertices of degree 4 and other vertices are of degree 3. Find the number of vertices in G. (5)

Q.6 (i) Consider a tree T with 3 vertices of degree 2, 4 vertices of degree 3 and 3 vertices of degree 4. Calculate the number of pendant vertices in a tree be  $m$ . (4)

(ii) Prove that there is one and only one path between every pair of vertices in a tree T. (4)

(iii) Define minimal spanning tree. Describe Prim's algorithm and use this to find out the minimal spanning tree of the following graph. (7)

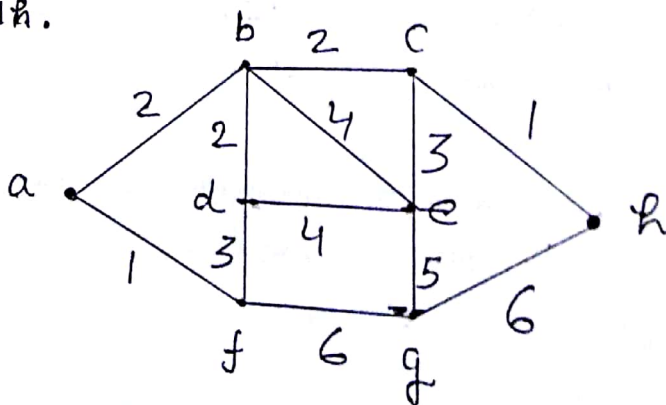


Q.7. (i) Define Eulerian Graph. Answer and justify

(a) which complete bipartite graphs are Eulerian?

(b) for what value of  $n$  is the graph of  $K_n$  Eulerian? (5)

(ii) Apply Dijkstra's algorithm to the graph given below and find the shortest path between  $a$  and  $h$ . (10)



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