

**M.Sc. (MATHEMATICS) – Semester I**

COURSE CODE	COURSE NAME	Course Type	Course Nature	PERIODS			CREDITS
		Core(Departmental/Allied)/ Elective (Departmental/ Open) / University Compulsory	Hard/Soft/ Workshop/ NTCC	L	P	O	
MAH501-T	ABSTRACT ALGEBRA	Core (Departmental)	Hard	4	0	0	4
MAH502-T	TOPOLOGY	Core (Departmental)	Hard	4	0	0	4
MAH503-T	DIFFERENTIAL EQUATION	Core (Departmental)	Hard	4	0	0	4
MAH504-T	GRAPH THEORY	ELECTIVE (Departmental) (Any one)	Hard	4	0	0	4
MAH505-T	OPERATIONS RESEARCH		Hard	4	0	0	
MAH506-T	MATHEMATICAL MODELING AND SIMULATION		Hard	4	0	0	
MAH507-p	MATHS LAB	Core (Departmental)	Hard	0	4	0	2
MAW508 MAW509 MAW231 MAW225 MAW119 CSW102	BASKET OF WORKSHOP ELECTIVES (ANY ONE)	Core (Departmental & Allied)	WORKSHOP	0	3	0	2
	RESEARCH METHODOLOGY	Core	SOFT	1	2	0	2

**BASKET OF WORKSHOP ELECTIVES (ANY ONE):** 1) SCILAB —MAW508  
 2) STATISTICS USING EXCEL —MAW119  
 3) MATHEMATICA--MAW509  
 4) SPSS —MAW231  
 5) LATEX—MAW225  
 6) HTML5 & CSS-CSW102

**DETAILED SYLLABUS  
SEMESTER I**

<b>Course Title/ Code</b>	<b>ABSTRACT ALGEBRA- MAH501-T</b>
<b>Course Type:</b>	Core (Departmental)
<b>Course Nature:</b>	Hard
<b>L-P-O Structure</b>	(4-0-0)
<b>Objective</b>	The student would be able to conceptualize and apply the concepts of Modern Algebraic Structures.

	<b>Sections</b>	<b>Weightage</b>
<b>Syllabus</b>	A	25%
	B	25%
	C	25%
	D	25%
	<b>TOTAL</b>	<b>100%</b>

**Section A**

Sylow's P-subgroups, Sylow's Theorems, Simple groups, Solvable groups, Nilpotent groups, Simplicity of Alternating Groups, Normal and Subnormal series, Composition series, Jordan-Holder Theorem. Direct product of groups, Structure theorem for finitely generated Abelian Groups.

**Section B**

Rings, Ring extensions; Polynomial rings, Formal power series rings, Matrix rings, Group rings, Ideals; Prime and Maximal ideals, Rings of fractions, Chinese Remainder Theorem for pairwise comaximal ideals.

**Section C**

Euclidean Domains, Principal Ideal Domains and Unique Factorizations Domains. Poly-nomial rings over UFD's.

**Section D**

Fields, Characteristic and prime subfields, Field extensions, Finite, Algebraic and Finitely generated field extensions, Classical ruler and compass constructions, Splitting fields, Finite fields, Cyclotomic fields, Separable and Inseparable extensions.

**Recommended Books:**

1. I.N. Herstein, Topics in Algebra
2. M. Artin, Algebra, Prentice Hall of India, 1994.
3. D.S. Dummit and R. M. Foote, Abstract Algebra, 2nd Ed., John Wiley, 2002.
4. I.B.S. Passi, Group Theory
5. I.B.S. Passi, Ring Theory
6. J.A. Gallian, Contemporary Abstract Algebra, 4th Ed., Narosa, 1999.
7. N. Jacobson, Basic Algebra I, 2nd Ed., Hindustan Publishing Co., 1984, W.H. Freeman, 1985.

<b>Course Title/ Code</b>	<b>TOPOLOGY-I- MAH502-T</b>
<b>Course Type:</b>	Core (Departmental)
<b>Course Nature:</b>	Hard
<b>L-P-O Structure</b>	(4-0-0)
<b>Objective</b>	The student would be able to conceptualize and apply the concepts of Topological Spaces.

	<b>Sections</b>	<b>Weightage</b>
<b>Syllabus</b>	A	25%
	B	25%
	C	25%
	D	25%
	<b>TOTAL</b>	<b>100%</b>

#### **Section A**

Definition and Examples of Topological spaces, Closed set, Closure, Dense subset, Neighborhoods, Interior, Exterior and Boundary, Accumulation point and Derived sets, Bases Sub-bases, Sub space and Relative topology.

#### **Section B**

Characterization of topology in terms of base and subbase axioms, Topology generated by a family of subsets, Alternate methods of defining a topology in term of Kuratowski closure Operator and Neighbourhood System, Continuous functions and Homomorphism.

#### **Section C**

First and Second Countable spaces, Lendelof's theorem, Separable spaces, Second count ability and Separability, Separation axioms  $T_0, T_1, T_2, T_3, T_4$ , Their Characterizations and basic Properties, Urysohn's lemma, Teitze extension theorem.

#### **Section D**

Compactness, Continuous functions and Compact sets, Basic properties of Compactness, Compactness and finite intersection property, Sequentially and countably compact sets, Connected spaces, Connectedness on the real line, Components, Locally connected space.

#### **Recommended Books:**

1. James R. Munkres, Topology (2ndEdition) Pearson Education Pve. Ltd., Delhi-2002
2. George F.Sinmons, Introduction to Topology and Modern Analysis, McGraw Hill Book Co., 1963
3. J. Dugundji , Topology , Prentice Hall of India, New Delhi, 1975.
4. K. D. Joshi : Introduction to General Topology (Wiley Eastern Limited).
5. S. Kumaresan: Topology of Metric Spaces, alpha science.

<b>Course Title/ Code</b>	<b>DIFFERENTIAL EQUATIONS-MAH503-T</b>
<b>Course Type:</b>	CORE (Departmental)
<b>Course Nature:</b>	Hard
<b>L-P-O Structure</b>	(4-0-0)
<b>Objective</b>	The student would be able to apply the concepts of Differential Equations in various physical problems.

	<b>Sections</b>	<b>Weightage</b>
<b>Syllabus</b>	A	25%
	B	25%
	C	25%
	D	25%
	<b>TOTAL</b>	<b>100%</b>

#### **SECTION-A**

Existence and Uniqueness of Ordinary Differential equations, Picard's method, Sturm comparison and separation theorems, System of first order non homogeneous equations, Homogeneous Linear system, Non-homogeneous Linear system, Linear system with constant coefficient, Two point boundary value problems, Green functions, Sturm-Liouville System, Eigen value and Eigen functions.

#### **SECTION-B**

Stability of autonomous system of differential equation, Types of critical points, Critical points and Stability of linear systems, stability by Liapunov's Direct method, Simple critical points of nonlinear systems, Nonlinear mechanics, Periodic solutions, The Poincare – Bendixson Theorem.

#### **SECTION-C**

Solution of Cauchy's problem of First order Partial Differential equations, Solution of Non-homogeneous PDE by Jacobi's method, PDE of the Second order (Homogeneous and Non-Homogeneous), Monge's Method, Method of separation of variables, Method of Integral transform.

#### **SECTION-D**

Laplace Equation in two dimension, Green function for Laplace Equation, Dirichlet and Newman problem for Half plane, Dirichlet and Newman problem for circle, Dirichlet and Newman problem for sphere and semi-infinite space, Wave Equation, Diffusion equation.

#### **Recommended Books:**

1. G. F. Simmons: Differential equation with Application and Historical Notes, McGraw-Hill
2. Ian Sneddon: Elements of Partial Differential Equations, McGraw-Hill.
3. S. L. Ross: Differential Equations, Wiley India.
4. M. D. Raisinghania : Advance Differential equation, S.Chand India.

<b>Course Title/ Code</b>	<b>GRAPH THEORY- MAH504-T</b>
<b>Course Type:</b>	ELECTIVE (Departmental)
<b>Course Nature:</b>	Hard
<b>L-P-O Structure</b>	(4-0-0)
<b>Objective</b>	The objective of the course is to introduce students with the fundamental concepts in graph Theory, with a sense of some its modern applications.

	<b>Sections</b>	<b>Weightage</b>
<b>Syllabus</b>	A	25%
	B	25%
	C	25%
	D	25%
	<b>TOTAL</b>	<b>100%</b>

#### **Section A**

Fundamental concepts: Definitions and examples, Graphs as models, Matrices and isomorphism, Paths, Connected graphs, Bipartite graphs, Extremality vertex degree, The Pigeonhole principal, Turan`s theorem, Degree sequences, Graphic sequences, Degree and digraphs.

#### **Section B**

Tree and Distances: Properties of tree, Distance in graphs, Stronger results, Disjoint spanning trees, Shortest paths, Trees in computer science, Eulerian circuits.

#### **Section C**

Matching and Factors: Matching in bipartite graphs, Maximum matchings, Hall`s matching conditions, Minimum Matching in bipartite graphs, Sets, Applications and algorithms, Maximum bipartite matching, Weighted bipartite matching, In general graphs, Tutte`s 1-factor theorem, F-factors of graphs.

#### **Section D**

Connectivity and Paths: Cuts, Connectivity, Edge-connectivity, Blocks, 2-connected graphs, Connectivity of digraphs, K connected and k-edge connected graphs, Applications of Menger`s theorem, Network flow problems maximum network flow, Integral flows.

#### **Recommended Books:**

1. Douglas B. West, Introduction to Graph Theory Prentice- Hall, New Delhi (1999)
2. John Clarke and D.A. Holton, A First Look at Graph Theory, Allied Publisher (1991).
3. Nora Harsfield and Gerhard Ringel, Pearls Theory, Academic Press (1990).
4. Harary, Graph Theory, Narosa Publishers, New Delhi (1989).

<b>Course Title/ Code</b>	<b>OPERATIONS RESEARCH- MAH505-T</b>
<b>Course Type:</b>	Elective (Departmental)
<b>Course Nature:</b>	Hard
<b>L-P-O Structure</b>	(4-0-0)
<b>Objective</b>	The student would be able to apply the concepts of Operations Research in various real time problems.

	<b>Sections</b>	<b>Weightage</b>
<b>Syllabus</b>	A	25%
	B	25%
	C	25%
	D	25%
	<b>TOTAL</b>	<b>100%</b>

#### **Section A**

Convex set theory: Linear independence and dependence of vectors, Convex sets, Extreme points, Hyper planes and Halfspaces, Directions of a convex set, Convex cones, Polyhedral sets and cones.

#### **Section B**

Introduction to Linear Programming: Linear Programming Problem Formulation, Graphical solution, Simplex Algorithm, Artificial variables techniques: Two-phase method & Big-M method , Duality theory, Dual-simplex method.

#### **Section C**

Transportation problem & Assignment problems: Formulation of Transportation problem, Optimal solution, Unbalanced transportation problem, Degeneracy, Formulation of Assignment problem, Optimal solution, Variants of Assignment Problem- Traveling Salesman problem.

#### **Section D**

Game Theory: Introduction, Two person zero sum game, Pure strategies, Maximin & miimax principle, Game with saddle points, Mixed strategies, Game without saddle points, Dominance rule.

#### **Recommended Books:**

1. H. A. Taha, Operations Research an introduction, pearson India
2. J. K. Sharma, Operations Research theory & applications:
3. Gupta & Hira, Operations Research.

<b>Course Title/ Code</b>	<b>MATHEMATICAL MODELING &amp; SIMULATIONS- MAH506-T</b>
<b>Course Type:</b>	ELECTIVE (Departmental)
<b>Course Nature:</b>	Hard
<b>L-P-O Structure</b>	(4-0-0)
<b>Objective</b>	The student would be able to apply the concepts of Mathematical Modeling and Simulations in various physical problems.

#### **Section A**

Mathematical Model, Types of Mathematical models and properties, Procedure of modeling, Graphical method: Bartering model, Basic optimization.

#### **Section B**

Basic probability: Monte-Carlo simulation, Approaches to differential equation: Heun method, Local stability theory: Bernoulli Trials, Classical and continuous models, Case studies in problems of engineering and biological sciences.

#### **Section C**

General techniques for simulating continuous random variables, Simulation from Normal and Gamma distributions.

#### **Section D**

Simulation from discrete probability distributions, Simulating a non- Homogeneous Poisson Process and Queuing system.

#### **Recommended Books:**

1. Edward A. Bender.. An Introduction to Mathematical Modeling.
2. A. C. Fowler.. Mathematical Models in Applied Sciences, Cambridge University Press.
3. J. N. Kapoor.. Mathematical Modeling, Wiley eastern Limited.
4. S.M. Ross ..Simulation, India Elsevier Publication.
5. A.M.Law and W.D.Kelton.. Simulation Modeling and Analysis, T.M.H. Edition.

<b>Course Title/ Code</b>	<b>MATHS LAB- MAW507-P</b>
<b>Course Type:</b>	Core (Departmental)
<b>Course Nature:</b>	Hard
<b>L-P-O Structure</b>	(0-4-0)
<b>Objective</b>	The student would be able to apply the tools of Matlab software for solving mathematical problems.

### LAB EXERCISE:

1. Introduction to MATLAB and use of some simple MATLAB commands.
2. Introduction to some of the fundamentals of MATLAB: Variables, operators, expressions and Arrays(including vectors and matrices)
3. Introduction to graphics: Basic Two-Dimensional Graphs, Labels, Multiple plots on the same axes, Line styles, Markers and color, Axis limits and Subplots.
4. Introduction to graphics: Three-Dimensional Graphs, Labels, Multiple plots on the same axes, Line styles, Markers and color, Axis limits and Subplots.
5. To find the Rank of a matrix, Inverse of a Square matrix and to reduce a matrix into Normal Form.
6. To solve the system of simultaneous linear equations. To find the Eigen values and Eigen vectors of a square matrix.
7. To find derivatives, partial derivatives & directional derivatives of functions.
8. To find limit, continuity & differentiability of function of single variable.
9. To find limit, continuity & differentiability of function of several variables.
10. To find maxima & minima of function of single & several variables.
11. Evaluation of Single, Double integral and Triple Integration.
12. To find the Surface area and volume of solids of revolution by single & double integration.
13. To solve ODE & LDE & plot the graph of the solution of LDE. Also, solve the linear differential equations with variable coefficients(Cauchy & Legendre Differential equations).
14. To solve & plot solutions the system of two & three ordinary differential equations.
15. To find gradient of a scalar field (through graph also). Also, find directional derivatives, divergence & curl (through graph also).



<b>Course Title/ Code</b>	<b>SCILAB- MAW508</b>
<b>Course Type:</b>	Core (Departmental)
<b>Course Nature:</b>	Workshop
<b>L-P-O Structure</b>	(0-3-0)
<b>Objective</b>	The student would be able to apply the tools of Scilab for solving various Mathematical Problems.

**LAB EXERCISE:**

1. Introduction to Scilab.
2. Scilab environment
3. Scilab as an interactive calculator
4. Scilab workspace and working directory
5. Creating matrices and some simple matrix operations
6. Sub-matrices
7. Statistics
8. Working with polynomials
9. Plotting graphs-2D & 3D.
10. Scilab programming language
11. Script files and function files
12. Writing Scilab functions
13. File operations

<b>Course Title/ Code</b>	<b>MATHEMATICA- MAW509</b>
<b>Course Type:</b>	Core (Departmental)
<b>Course Nature:</b>	Workshop
<b>L-P-O Structure</b>	(0-3-0)
<b>Objective</b>	The student would be able to apply the tools of Mathematica for solving various Mathematical Problems.

**LAB EXERCISE:**

1. Introduction to MATHEMATICA and use of some simple MATHEMATICA commands.
2. Introduction to some of the fundamentals of MATHEMATICA: Symbols & Variables, Dynamic Data typing, Assignments & Equality Checks, Logical operators, loops and four types of brackets in MATHEMATICA.
3. To study the working with lists in MATHEMATICA.
4. To study rules, patterns and functions.
5. To study functions on lists and functional programming.
6. Writing efficient programs: some techniques and applications.

<b>Course Title/ Code</b>	<b>SPSS WORKSHOP-MAW231</b>
<b>Course Type:</b>	Core (Departmental)
<b>Course Nature:</b>	Workshop
<b>L-P-O Structure</b>	(0-3-0)
<b>Objectives</b>	The student would be able to apply the concepts of SPSS for Data Analysis.

### LAB EXERCISE;

1. Introduction SPSS software, open and save an SPSS data file, define codes for categorical variables in SPSS, print a copy of an SPSS data file.
2. Categorize a quantitative variable, create a bar chart, create a pie chart.
3. Create a modified box plot of one quantitative variable, create modified box plots of one quantitative variable to compare groups, create modified box plots to compare quantitative variables.
4. Enter a contingency table into an SPSS data file, create a pie chart from a contingency table, create a stacked bar chart from a contingency table.
5. Create a contingency table from raw data entered into an SPSS data file, create a stacked bar chart from a contingency table.
6. Obtain the equation of the least squares line for predicting one quantitative variable from another quantitative variable create a graph of the least squares line on a scatter plot create a modified box plot of the residuals.
7. Enter data into an SPSS data file perform two sample t tests and create appropriate graphical displays.
8. Perform a one sample paired t test and create an appropriate graphical display.
9. Enter data into an SPSS data file, perform a one-way analysis of variance and create and an appropriate graphical display.
10. Perform a chi-square goodness-of-fit test and create and appropriate graphical display create a stacked bar chart from a contingency table.

<b>Course Title/ Code</b>	<b>LaTeX -MAW225</b>
<b>Course Type:</b>	Core (Departmental)
<b>Course Nature:</b>	Workshop
<b>L-P-O Structure</b>	(0-3-0)
<b>Objective</b>	The students would be able to apply the concepts of LaTeX to create a document of Scientific Writing.

### LAB EXERCISE:

1. Introduction and basics of LaTeX.
2. Document structure and text formatting in LaTeX.
3. Mechanics of error and warning, lengths, Counters and Boxes.
4. Fundamentals for creating Technical Texts.
5. To Create Special Pages: Indexing ,Glossary, Bibliography
6. To Create Special Documents: Letters, Presentations, Curriculum Vitae.
7. Creating Graphics in LaTeX.
8. Programming: Macros, Plain text, Creating Packages, Themes.
9. Miscellaneous: Modular Documents, Collaborative Writing of LaTeX Documents, Export to other Formats.
10. Math – Type in Microsoft Word.

<b>Course Title/ Code</b>	<b>STATISTICAL METHODS USING EXCEL- MAW119</b>
<b>Course Type:</b>	Core (Departmental)
<b>Course Nature:</b>	Workshop
<b>L-P-O Structure</b>	(0-3-0)
<b>Objective</b>	The student would be able to apply the concepts of statistics for solving mathematical problems using Excel.

### **LAB EXERCISE**

1. To present the data by tables and by diagrams. To study the frequency distributions by histogram and frequency polygon.
2. To find mean, median, mode, quartiles, deciles and percentiles for the data.
3. To find mean deviation, standard deviation, coefficient of mean deviation and coefficient of variation. Comparison of various measures of dispersion.
4. To find moments, coefficient of skewness and measures of kurtosis.
5. Bivariate data scatter diagram, principle of least squares and fitting of polynomials and exponential curves.
6. To find coefficient of correlation and rank correlation. Multiple correlation analysis.
7. To find regression coefficients and lines of regression.
8. To construct the index numbers by different methods. Time reversal, factor reversal and circular tests.
9. Analysis of time series by using different methods (graphical method, method of semi averages, method of fitting curves).
10. To study Sampling distributions. Tests of significance based on t and F distributions.
11. Test of significance based on Chi- square distribution.

**M.Sc. (MATHEMATICS)- Semester II**

COURSE CODE	COURSE NAME	Course Type	Course Nature	PERIODS			CREDITS
		Core(Departmental/Allied)/ Elective (Departmental/ Open) / University Compulsory	Hard/Soft/ Workshop/ NTCC	L	P	O	
MAH510-T	ADVANCED LINEAR ALGEBRA	Core (Departmental)	Hard	4	0	0	4
MAH511-T	COMPLEX ANALYSIS	Core (Departmental)	Hard	4	0	0	4
MAH512-T	MEASURE THEORY	Core (Departmental)	Hard	4	0	0	4
MAH513-T	FUZZY SETS & FUZZY LOGIC	ELECTIVE (Departmental) (Any one)	Hard	4	0	0	4
MAH514-T	MATHEMATICAL STATISTICS		Hard	4	0	0	
MAH515-T	TOPOLOGY-II		Hard	4	0	0	
MAH516-P	MATHS LAB	Core (Departmental)	Hard	0	4	0	2
MAW508 MAW509 MAW231 MAW225 MAW119 CSW102	BASKET OF WORKSHOP ELECTIVES(ANY ONE)	ELECTIVE(Departmental)	WORKSHOP	0	3	0	2
	PEDAGOGICAL SKILLS	Core	SOFT	1	2	0	2

**BASKET OF WORKSHOP ELECTIVES (ANY ONE):** 1) SCILAB —MAW508  
 2) STATISTICS USING EXCEL —MAW119  
 3) MATHEMATICA--MAW509  
 4) SPSS —MAW231  
 5) LATEX—MAW225  
 6) HTML5 & CSS-CSW102

\*\* MAW517---SUMMER TRAINING

**DETAILED SYLLABUS  
SEMESTER II**

<b>Course Title/ Code</b>	<b>ADVANCED LINEAR ALGEBRA- MAH510-T</b>
<b>Course Type:</b>	Core (Departmental)
<b>Course Nature:</b>	Hard
<b>L-P-O Structure</b>	(4-0-0)
<b>Objective</b>	The student would be able to conceptualize and apply the concepts of Advanced Linear Algebra.

	<b>Sections</b>	<b>Weightage</b>
<b>Syllabus</b>	A	25%
	B	25%
	C	25%
	D	25%
	<b>TOTAL</b>	<b>100%</b>

**Section A**

Characteristic values and Characteristic vectors of linear transformations, Minimal polynomial for linear transformation, Invariant Subspaces, Simultaneous triangulation and Simultaneous diagonalization Similarity of linear transformations, Representation by a diagonal matrix, Direct -Sum decompositions and Invariant direct Sums, The primary decomposition theorem.

**Section B**

The Rational canonical forms and Jordan canonical forms; Cyclic subspaces and Annihilators, The Rational canonical form, Cyclic decomposition theorem, The Jordan blocks and Jordan canonical form.

**Section C**

Inner Product Spaces; Definition of inner product spaces, Euclidean space, Unitary space, Cauchy-Schwarz inequality, Orthogonal and orthonormal set, Gram-Schmidt orthogonalization theorem, Orthogonal complement, Linear functionals and Adjoints; Self-adjoint (Hermitian), Unitary operators, Normal operators, Operators on inner product spaces; Forms on inner product spaces, Positive form, Spectral theorem.

**Section D**

Bilinear Forms; Bilinear form, Non-degenerate bilinear form, Symmetric bilinear form and Skew-symmetric bilinear form. Quadratic forms; Real quadratic forms, Orthogonal matrices, Reduction of real quadratic forms, Nilpotent forms, Classification of real quadratic forms.

**Recommended Books:**

1. K. Hoffman and R. Kunze, Linear Algebra, Pearson Education (India), 2003. Prentice-Hall of India, 1991.
2. S. Lang, Linear Algebra, Undergraduate Texts in Mathematics, Springer-Verlag, New York, 1989.
3. I. N. Herstein, Topic in Abstract Algebra, Wiley Eastern Limtd.
4. A.G. Hamilton, Linear Algebra, Cambridge University Press (1989)

<b>Course Title/ Code</b>	<b>COMPLEX ANALYSIS-MAH511-T</b>
<b>Course Type:</b>	Core (Departmental)
<b>Course Nature:</b>	Hard
<b>L-P-O Structure</b>	(4-0-0)
<b>Objective</b>	The objective of this course is to introduce the fundamental ideas of developing a clear understanding of the fundamental concepts of Complex Analysis such as analytic functions, complex integrals and conformal mapping.

	<b>Sections</b>	<b>Weightage</b>
<b>Syllabus</b>	A	25%
	B	25%
	C	25%
	D	25%
	<b>TOTAL</b>	<b>100%</b>

#### **Section A**

Complex Integration, Cauchy-Goursat Theorem, Cauchy's Integral Theorem, Cauchy's Integral Formula, Cauchy's Integral Formula for Higher order derivatives, Morera's Theorem, Cauchy's Inequality and Liouville's theorem, The Fundamental theorem of algebra.

#### **Section B**

Taylor & Laurent's Series Expansion, Isolated Singularities, Casporati-Weierstress theorem, Meromorphic functions, The argument principle, Rouche's theorem, Inverse function theorem. Residues, Cauchy's residue theorem, Evaluation of integrals, Branches of many valued functions with special reference to  $\arg Z$ ,  $\log Z$ , and  $Z^a$ .

#### **Section C**

Analytic continuation, Uniqueness of direct analytic continuation, Uniqueness of analytic continuation along a curve, Power series method of analytic continuation, Schwarz reflection principle, Monodromy theorem and its consequences.

#### **Section D**

Conformal Mapping, general linear transformations, Analytic- continuation, Principle of reflection, Principle of maximum modulus, Searz's lemma, Vitali's convergence theorem, Hadamard's three circle theorem functions.

#### **Recommended Books:**

1. Prof R.Y. Dennis, Complex- Variable & integral transform.
2. S. Ponnusamy, Complex Analysis.
3. E. T. Copson, Complex Variables, Oxford University Press.
4. J. B. Conway, Functions of one complex variable, Narosa Publication House.



<b>Course Title/ Code</b>	<b>MESURE THEORY- MAH512-T</b>
<b>Course Type:</b>	Core (Departmental)
<b>Course Nature:</b>	Hard
<b>L-P-O Structure</b>	(4-0-0)
<b>Objective</b>	The student would be able to conceptualize measure and integral with respect to a measure and apply the concepts of measure theory for further studies in Analysis, probability and dynamical systems etc.

	<b>Sections</b>	<b>Weightage</b>
<b>Syllabus</b>	A	25%
	B	25%
	C	25%
	D	25%
	<b>TOTAL</b>	<b>100%</b>

#### **Section A**

Boolean algebra, Borel field, Counting measure, Outer measure, Measurable sets, Lebesgue measure, non-measurable sets, Measurable functions, Littlewood's Three principles.

#### **Section B**

Riemann Integral, Lebesgue Integral of a Bounded functions over a set of Finite Measure, Fatou's Lemma, Monotone Convergence Theorem, Lebesgue Convergence Theorem and Convergence in Measure.

#### **Section C**

Vitali's Lemma Functions of Bounded variation, Absolute continuity, Converse functions, Jensen Inequality, Measure spaces,  $\sigma$ -finite measure, Semifinite measure, General convergence Theorems, Signed Measures, Hahn Decomposition Theorem, Jordan decomposition, Radon-Nikodym Theorem, Lebesgue decomposition, Product measure, Fubini's Theorem.

#### **Section D**

The  $L^p$  spaces where  $1 \leq p < \infty$ , Holder and Minkowski inequalities, Completeness of  $L_p$  spaces.

#### **Recommended Books:**

1. Real Analysis : H. L. Royden
2. Mathematical Analysis : T. M. Apostol
3. Real Analysis : Walter Rudin
4. Real and Abstract Analysis : E. Hewitt and K. Stromberg

<b>Course Title/ Code</b>	<b>FUZZY SETS &amp; FUZZY LOGIC- MAH513-T</b>
<b>Course Type:</b>	Elective(Departmental)
<b>Course Nature:</b>	Hard
<b>L-P-O Structure</b>	(4-0-0)
<b>Objective</b>	The student would be able to conceptualize basic knowledge of fuzzy sets and fuzzy logic and apply these concepts for basic fuzzy system modeling methods & PID control systems.

	<b>Sections</b>	<b>Weightage</b>
<b>Syllabus</b>	A	25%
	B	25%
	C	25%
	D	25%
	<b>TOTAL</b>	<b>100%</b>

#### **Section A**

Fuzzy Sets: Basics Classical sets vs Fuzzy Sets , Need for fuzzy sets , Definition and Mathematical representations , Level Sets, Fuzzy functions , Zadeh's Extension Principle.

#### **Section B**

Operations on Fuzzy Sets: Operations on  $[0,1]$  – Fuzzy negation, Triangular norms, T-conorms, Fuzzy implications, Aggregation Operations, Fuzzy Functional Equations

#### **Section C**

Fuzzy Relations: Fuzzy Binary and n-ary relations, composition of fuzzy relations , Fuzzy Equivalence Relations, Fuzzy Compatibility Relations, Fuzzy Relational Equations.

#### **Section D**

Fuzzy Logic: Basic concepts of Fuzzy logic, Linguistic variables, Membership functions, , Fuzzy if-then rules, Variables inference techniques, Defuzzification techniques, Basic Fuzzy inference algorithm, Applications of fuzzy logic.

#### **Recommended Books:**

1. H.J. Zimmermann, Fuzzy Set Theory and its Applications, Allied Publishers, New Delhi, 1991
2. Timothy J. Ross, "Fuzzy Logic with Engineering Applications," McGraw Hill, 1995.
3. Kevin M Passino and Stephen Yurkovich, Fuzzy Control, Addison Wesley Longman, 1998.
4. Michal Baczynski and Balasubramaniam Jayaram, Fuzzy Implications, Springer Verlag, Heidelberg, 2008.

<b>Course Title/ Code</b>	<b>MATHEMATICAL STATISTICS-MAH514-T</b>
<b>Course Type:</b>	Elective(Departmental)
<b>Course Nature:</b>	Hard
<b>L-P-O Structure</b>	(4-0-0)
<b>Objective</b>	The student would be able to apply the concepts of statistics for solving mathematical problems and its applications.

	<b>Sections</b>	<b>Weightage</b>
<b>Syllabus</b>	A	25%
	B	25%
	C	25%
	D	25%
	<b>TOTAL</b>	<b>100%</b>

#### **Section A**

Probability and Baye's Theorem, Random Variables, Probability Density Functions, Multivariate Distributions, Marginal Distributions, Conditional Distributions, Mathematical Expectation, Moments, Moment Generating Functions, Product Moments, The Binomial Distribution, The Poisson Distribution, The Normal Distribution, Correlation and Regression.

#### **Section B**

Special Probability Distributions: The Discrete Uniform Distribution, The Negative Binomial and Geometric Distributions, The Hypergeometric Distribution, The Multinomial Distribution, The Multivariate Hypergeometric Distribution, Special Probability Densities: The Uniform Distribution, The Gamma, Exponential and Chi-Square Distributions, The Beta Distribution, The Normal approximation to the Binomial Distribution, The Bivariate Normal Distribution.

#### **Section C**

Sampling Distributions & Decision Theory: Point Estimation, Interval Estimation, The Distribution of the mean – finite Populations, Hypothesis Testing, Tests of Hypothesis involving Mean, Variance and Proportions, The Chi-Square Distribution, The t – Distribution, The F – Distribution, Order Statistics.

#### **Section D**

The Theory of Games, Statistical Games, the Minimax Criterion.

Design and Analysis of Experiments: Introduction, One – Way Designs, Randomized – Block Designs, Factorial Experiments, Multiple Comparisons and Other Experimental Designs. Non- Parametric Tests: The Sign Test, The Signed – Rank Test, and Rank Sum Tests: The U Test and H Test, Tests Based on Runs.

#### **Recommended Books:**

1. Mood, A.M., Graybill, F.A. and Boes, D.C., Mc Graw Hill Book Company.
2. Freund, J.E., Mathematical Statistics, Prentice Hall of India.
3. Gupta S.C. and Kapoor V.K., Fundamentals of Mathematical Statistics, S.Chand Pub., New Delhi.

<b>Course Title/ Code</b>	<b>TOPOLOGY-II-MAH515-T</b>
<b>Course Type:</b>	Elective(Departmental)
<b>Course Nature:</b>	Hard
<b>L-P-O Structure</b>	(4-0-0)
<b>Objective</b>	The student would be able to conceptualize and apply the concepts of Topological Spaces.

	<b>Sections</b>	<b>Weightage</b>
<b>Syllabus</b>	A	25%
	B	25%
	C	25%
	D	25%
	<b>TOTAL</b>	<b>100%</b>

#### **Section A**

Tychonoff product topology in term of standard sub-base and its characterizations, Projection maps, Separation axioms and product spaces, Connectedness and product spaces, Compactness and product spaces, Countability and product spaces .

#### **Section B**

Nets and filters, Topology and convergence of nets, Housdorffness and nets , Compactness, Nets Filter and their Convergence.

#### **Section C**

Application of Urysohn's Lemma, The Stone–Cech Compactification, The Stone–Weierstrass Theorems.

#### **Section D**

Basic Algebraic Topology, Homotopy and the Fundamental Groups, Covering Spaces.

#### **Recommended Books:**

1. James R. Munkres, Topology (2ndEdition) Pearson Education Pve. Ltd., Delhi-2002
2. J. Dugundji , Topology , Prentice Hall of India, New Delhi, 1975.
3. George F.Sinmons, Introduction to Topology and Modern Analysis, McGraw Hill Book Co., 1963
4. K. D. Joshi : Introduction to General Topology (Wiley Eastern Limited).

<b>Course Title/ Code</b>	<b>MATHS LAB- MAH516-P</b>
<b>Course Type:</b>	Core (Departmental)
<b>Course Nature:</b>	Hard
<b>L-P-O Structure</b>	(0-4-0)
<b>Objective</b>	The student would be able to apply the tools of Matlab software for solving the Mathematical problems.

### LAB EXERCISE:

1. Introduction to programming.
2. Creating script file or m-files
3. Introduction to Conditional statements –if and else using MATLAB.
4. Introduction to Conditional statements –if and else using MATLAB (Continued).
5. Introduction to Loops- for using MATLAB.
6. Introduction to Loops- while using MATLAB.
7. Introduction to switch and break using MATLAB
8. Introduction to functions and function files using MATLAB.
9. Introduction to functions and function files using MATLAB (continued).
10. Study Linear Algebra using MATLAB.
11. Study Linear Algebra using MATLAB(Continued)

**M.Sc. (MATHEMATICS)- Semester-III**

COURSE CODE	COURSE NAME	Course Type	Course Nature	PERIODS			CREDITS
		Core(Departmental/Allied)/ Elective (Departmental/ Open) / University Compulsory	Hard/Soft/ Workshop/ NTCC	L	P	O	
MAH618-T	FUNCTIONAL ANALYSIS	Core (Departmental)	Hard	4	0	0	4
MAH619-T	DIFFERENTIAL GEOMETRY	Core (Departmental)	Hard	4	0	0	4
MAH620-T	DYNAMICS OF RIGID BODY	Core (Departmental)	Hard	4	0	0	4
MAH621-T	CODING THEORY	ELECTIVE (Departmental) (Any one)	Hard	4	0	0	4
MAH622-T	GENERAL THEORY OF RELATIVITY		Hard	4	0	0	
MAH623-T	ADVANCED OPERATIONS RESEARCH		Hard	4	0	0	
MAH624-T	FOURIER ANALYSIS		Hard	4	0	0	
MAH625-P	MATHS LAB	Core (Departmental)	WORKSHOP	0	4	0	2
	BASKET OF COURSES BY MANEGMENT DEPARTMENT	Elective (Allied)	SOFT	1	2	0	2
MAN626	SEMINAR	Core (Departmental)	NTCC	0	3	0	2

**DETAILED SYLLABUS  
SEMESTER III**

<b>Course Title/ Code</b>	<b>FUNCTIONAL ANALYSIS- MAH618-T</b>
<b>Course Type:</b>	Core (Departmental)
<b>Course Nature:</b>	Hard
<b>L-P-O Structure</b>	(4-0-0)
<b>Objective</b>	The student would be able to conceptualize basics of Functional Analysis and apply these concepts in harmonic analysis and stochastic calculus.

	<b>Sections</b>	<b>Weightage</b>
<b>Syllabus</b>	A	25%
	B	25%
	C	25%
	D	25%
	<b>TOTAL</b>	<b>100%</b>

**Section A**

Vector space, Normed linear space, Quotient space, Banach spaces, Bounded linear transformation,  $B(X,Y)$  as a normed linear space, Isometric isomorphism, Uniform boundedness principle and its consequences.

**Section B**

Hahn-Banach Theorem, Application of Hahn-Banach theorem, Conjugate and second conjugate space of normed linear space, Weak topology, Strong topology, Open-mapping theorem, Closed graph theorem, Uniform Boundedness theorem.

**Section C**

Inner Product Spaces, Hilbert spaces, Orthonormal sets, Bessel's Inequality, Complete orthonormal sets and Parseval's identity, Orthonormal bases, Structure of Hilbert space, Projection theorem, Riesz representation theorem, Riesz-Fischer theorem.

**Section D**

Adjoint of an operator on a Hilbert Space, Strong and weak convergence, Operator theory, Spectral theorem, Polar decomposition, Compact Operator, Fredholm Operators, Closed operators, Symmetric and self-adjoint operators.

**Recommended Books:**

1. V.S. Sunder, Functional Analysis spectral theory.
2. Walter Rudin, Functional Analysis.
3. S. Ponnusamy, Foundation of Functional Analysis.

<b>Course Title/ Code</b>	<b>DIFFERENTIAL GEOMETRY- MAH619-T</b>
<b>Course Type:</b>	Core (Departmental)
<b>Course Nature:</b>	Hard
<b>L-P-O Structure</b>	(4-0-0)
<b>Objective</b>	The student would be able to apply the concepts of space curves, geodesics, intrinsic and non-intrinsic properties of a surface.

	<b>Sections</b>	<b>Weightage</b>
<b>Syllabus</b>	A	25%
	B	25%
	C	25%
	D	25%
	<b>TOTAL</b>	<b>100%</b>

#### **Section A**

Co-ordinate transformation, Covariant, Contravariant and Mixed tensors, Tensors of higher rank, Symmetric and Skew-symmetric tensors, Tensor algebra, Contraction, Inner product, Riemannian metric tensor, Christoffel symbols, Covariant derivatives of tensors.

#### **Section B**

Differentiable curves in  $R^3$  and their parametric representations, Vector fields, Tangent vector, Principal normal, Binormal, Curvature and torsion, Serret-Frenet formula, Frame fields, Covariant differentiation, Connection forms, The structural equations.

#### **Section C**

Surfaces, Differentiable functions on surfaces, Differential of a differentiable map, Differential forms, Normal vector fields, First fundamental form, Shape operator, Normal curvature, Principal curvatures, Gaussian curvature, Mean curvature, Second fundamental form.

#### **Section D**

Gauss equations, Weingarten equation, Codazzi-Mainardi equations, Totally umbilical surfaces, Minimal surfaces, Variations, First and second variations of arc length, Geodesic, Exponential map, Jacobi vector field, Index form of a geodesic.

#### **Recommended Books:**

1. Barrett O' Neill, Elementary Differential Geometry, Academic Press, 2006.
2. Manfredo P. Do' Carmo, Differential Geometry of Curves and Surfaces, , Prentice Hall Inc.
3. S. Montiel and A. Ros, Curves and Surfaces , American Mathematical Society, 2005.
4. Somasundaram, Differential Geometry, A first course , Narosa Publication.
5. Zafar Ahsan, Tensor Calculus, Anamaya Publications, New Delhi. 19 / 27
6. U. C. De, Tensor Calculus, Narosa Publications, New Delhi.



<b>Course Title/ Code</b>	<b>DYNAMICS OF RIGID BODY- MAH620-T</b>
<b>Course Type:</b>	Core (Departmental)
<b>Course Nature:</b>	Hard
<b>L-P-O Structure</b>	(4-0-0)
<b>Objective</b>	To study mechanical systems under generalized coordinate systems, energy and momentum to study mechanics developed by Jacobian, Euler, Legendre, with Extremals and Functionals.

	<b>Sections</b>	<b>Weightage</b>
<b>Syllabus</b>	A	25%
	B	25%
	C	25%
	D	25%
	<b>TOTAL</b>	<b>100%</b>

#### **Section A**

Moments and products of inertia, The momental ellipsoid, Equipomental systems Principal axes, D'Alembert's principle, The general equation of motion of a rigid body, Motion of Centre of inertia and motion relative to the centre of inertia.

#### **Section B**

Motion about the fixed axis, The compound pendulum, Centre of Percussion, Motion of rigid body in two dimensions under finite and impulsive forces.

#### **Section C**

Conservation of Momentum and Energy, Initial motions, Lagrange's equation Euler's equations of motion, Hamilton's principle, Hamilton's equation of motion, Euler's equation for functional containing first order derivative and one independent variable, Extremals.

#### **Section D**

Functionals dependent on higher order derivatives Functional s dependent on more than one independent variable, Variational problems in parametric form, Invariance of Euler's equation under coordinate transformation, Jacobian and Legendre conditions, Second variation, Variational principle of least action.

#### **Recommended Books:**

1. D. Greenwood, Classical Dynamics, Prentice Hall of India, New Delhi, 1985.
2. H. Goldstein, Classical Mechanics, (2ndEdition) Narosa Publishing House, New Delhi.
3. A.S Gupta, Calculus of variations with –Applications, Prentice Hall of india, 1997
4. S.L. Loney, An elementary Treatise on the dynamics of particle and rigid bodies, Cambridge University Press.

<b>Course Title/ Code</b>	<b>CODING THEORY- MAH621-T</b>
<b>Course Type:</b>	Elective (Departmental)
<b>Course Nature:</b>	Hard
<b>L-P-O Structure</b>	(4-0-0)
<b>Objective</b>	The students would be able to apply the concepts of coding theory.

	<b>Sections</b>	<b>Weightage</b>
<b>Syllabus</b>	A	25%
	B	25%
	C	25%
	D	25%
	<b>TOTAL</b>	<b>100%</b>

#### **Section A**

The communication channel, The coding problem, Types of codes, Block codes, Error-detecting and error-correcting codes, Linear codes, The Hamming metric, Description of linear block codes by matrices, Dual codes, Standard array, Syndrome.

#### **Section B**

Step-by-step decoding, Modular representation, Error-correction capabilities of linear codes, Bounds on minimum distance for block codes, Plotkin bound, Hamming sphere packing bound, Varshamov-Gilbert-Sacks bound.

#### **Section C**

Bounds for burst-error detecting and correcting codes, Important linear block codes, Hamming codes.

#### **Section D**

Golay codes, Perfect codes, Quasi-perfect codes, Reed-Muller codes, Codes derived from Hadamard matrices, Product codes, Concatenated codes.

#### **Recommended Books:**

1. W.W. Peterson and E.J. Weldon, Jr., Error-Correcting Codes. M.I.T. Press, Cambridge, Massachusetts, 1972.
2. Raymond Hill, A First Course in Coding Theory, Oxford University Press, 1990.
3. Man Young Rhee, Error Correcting Coding Theory, McGraw Hill Inc., 1989.
4. F.J. Macwilliams and N.J. A. Sloane, The Theory of Error Correcting Codes, North- Holland, 2006.

<b>Course Title/ Code</b>	<b>GENERAL THEORY OF RELATIVITY- MAH622-T</b>
<b>Course Type:</b>	Elective (Departmental)
<b>Course Nature:</b>	Hard
<b>L-P-O Structure</b>	(4-0-0)
<b>Objective</b>	The students would be able to understand the fundamental principles of the general theory of relativity.

	<b>Sections</b>	<b>Weightage</b>
<b>Syllabus</b>	A	25%
	B	25%
	C	25%
	D	25%
	<b>TOTAL</b>	<b>100%</b>

#### **Section A**

Uniform vector field. Flat space-time, Review of the special theory of relativity and the Newtonian mechanics. The law of gravitation, Principle of equivalence and general covariance, Geodesic principle, Newtonian approximation relativistic equations of motion, Einstein's field equations and its Newtonian approximation, Schwarzschild external solution and its isotropic form.

#### **Section B**

Planetary orbits and analogues of Kepler's laws in general relativity, Advance of perihelion of a planet, Bending of light rays in a gravitational field, Gravitational redshift of spectral lines, Radar Echo delay, Schwarzschild internal solution, Energy momentum tensor of a perfect fluid.

#### **Section C**

Static Cosmological Models: Mach's principle, Einstein modified field equations with Cosmological term, Static cosmological models, Properties of Einstein model, Properties of De-sitter model, Difference between Einstein and De-sitter universe, Comparison of Einstein and De-sitter universes with actual universe.

#### **Section D**

Non-Static Cosmological Models: Weyl's postulate, Cosmological principles, Hubble's law, Derivation of Robertson-Walker metric, Geometrical feature of RW metric, Redshift versus distance relation, Angular size versus redshift relation and source counts in Robertson-Walker space-time, Friedmann models, Particle horizon, Event horizon, Einstein's equation and dynamics of the universe.

#### **Recommended Books:**

1. J. N. Islam, A Introduction to Mathematical Cosmology, Cambridge University Press.
2. J.V. Narlikar, General Relativity and Cosmology, The Macmillan Company of India Limited, 1978.
3. S.R Roy & Raj Bali, Theory of Relativity
4. A.S. Eddington, The Mathematical Theory of Relativity, Cambridge University Press, 1965.
5. P.G. Bergmann, Introduction to the Theory of Relativity

<b>Course Title/ Code</b>	<b>ADVANCED OPERATIONS RESEARCH- MAH623-T</b>
<b>Course Type:</b>	Elective (Departmental)
<b>Course Nature:</b>	Hard
<b>L-P-O Structure</b>	(4-0-0)
<b>Objective</b>	The student would be able to apply the concepts of Operations Research in various real time problems.

	<b>Sections</b>	<b>Weightage</b>
<b>Syllabus</b>	A	25%
	B	25%
	C	25%
	D	25%
	<b>TOTAL</b>	<b>100%</b>

#### **Section A**

**Project management-PERT & CPM:** Significance, Phases of project management, PERT /CPM network components and precedence relationship, Critical path analysis, Forward and backward pass methods, Slack of an activity and event, Project scheduling with uncertain activity times, Estimation of project completion time, Project time –cost trade off, Updating of the project progress.

#### **Section B**

**Replacement:** Introduction, Replacement of items that deteriorate with time – when money value is not counted and counted – Replacement of items that fail completely, Group replacement, Staffing problem, Equipment renewal problem.

#### **Section C**

**Queuing Theory:** Introduction, Single Channel, Poisson arrivals, Exponential service times – with infinite population and finite population models, Multichannel, Poisson arrivals, exponential service times with infinite population single channel Poisson arrivals.

#### **Section D**

**Quadratic Programming:** Wolfe's method, Complementary pivot algorithm, Duality in quadratic programming.

#### **Recommended Books:**

1. H. A. Taha, Operations Research an introduction, pearson India
2. J. K. Sharma, Operations Research theory & applications:
3. Gupta & Hira, Operations Research,

<b>Course Title/ Code</b>	<b>FOURIER ANALYSIS- MAH624-T</b>
<b>Course Type:</b>	Elective (Departmental)
<b>Course Nature:</b>	Hard
<b>L-P-O Structure</b>	(4-0-0)
<b>Objective</b>	The student would be able to apply the concepts of discrete Fourier series, integral Fourier and Inverse - Fourier transforms for solving mathematical problems.

	<b>Sections</b>	<b>Weightage</b>
<b>Syllabus</b>	A	25%
	B	25%
	C	25%
	D	25%
	<b>TOTAL</b>	<b>100%</b>

#### **Section A**

Basic Properties of Fourier Series: Uniqueness of Fourier Series, Convolutions, Cesaro and Abel Summability, Fejer's theorem, Poisson Kernel and Dirichlet problem in the unit disc, Mean square Convergence, Example of Continuous functions with divergent Fourier series.

#### **Section B**

L2-theory: Orthogonality, Completeness, ON systems, Applications to partial differential equations, Separation of variables, Something about Sturm-Liouville theory and Eigen function expansions.

#### **Section C**

Distributions and Fourier Transforms: Calculus of Distributions, Schwartz class of rapidly decreasing functions, Fourier transforms of rapidly decreasing functions, Riemann Lebesgue lemma, Fourier Inversion Theorem, Fourier transforms of Gaussians.

#### **Section D**

Tempered Distributions: Fourier transforms of tempered distributions, Convolutions, Applications to PDEs (Laplace, Heat and Wave Equations), Schrodinger-Equation and Uncertainty principle.

Paley-Wiener Theorems, Poisson Summ-ation Formula: Radial Fourier transforms and Bessel's functions, Hermite functions.

#### **Recommended Books:**

1. R. Strichartz, A Guide to Distributions and Fourier Transforms, CRC Press.
2. E.M. Stein and R. Shakarchi, Fourier Analysis: An Introduction, Princeton University Press, Princeton 2003.

<b>Course Title/ Code</b>	<b>MATHS LAB- MAH625-P</b>
<b>Course Type:</b>	Core (Departmental)
<b>Course Nature:</b>	Hard
<b>L-P-O Structure</b>	(0-4-0)
<b>Objective</b>	The student would be able to apply the tools of Matlab software for solving the concepts of Mathematical problems.

### LAB EXERCISE:

1. Introduction to Maple and Methods of entering expressions.
2. An introduction to the point-and-click features in Maple and An introduction to the commands of the Maple Language.
3. Entering and evaluating mathematical expressions in Document mode.
4. Worksheet mode – input prompt and commands.
5. Pallets
6. Introduction to graphs, graphs of Tabular and continuous functions.
7. Graphs of composed functions.
8. To solve standard mathematical problems.
9. To construct and compute with expressions that have units, scientific constants or uncertainty.
10. To evaluate plane curves in rectangular coordinates using Maple.
11. To evaluate curve in polar coordinates using Maple.
12. To calculate asymptotes of curves using Maple.
13. To calculate tangent lines to curve, singular points on curves using Maple.
14. To calculate curvature and torsion of curves using Maple.

**M.Sc. (MATHEMATICS)- Semester-IV**

COURSE CODE	COURSE NAME	Course Type	Course Nature	PERIODS			CREDITS
		Core(Departmental/Allied)/ Elective (Departmental/ Open) / University Compulsory	Hard/Soft/ Workshop/ NTCC	L	P	O	
MAH627-T	WAVELET ANALYSIS	Core (Departmental)	Hard	4	0	0	4
MAH628-T	FLUID MECHANICS	Core (Departmental)	Hard	4	0	0	4
MAH629-T	ALGEBRAIC TOPOLOGY	ELECTIVE (Departmental) (Any one)	Hard	4	0	0	4
MAH630-T	CRYPTOGRAPHY		Hard	4	0	0	
MAH631-T	STRUCTURES ON DIFFERENTIABLE MANIFOLDS						
MAH632-T	THEORY OF ELASTICITY & FRACTURE MECHANICS		Hard	4	0	0	
MAH633-P	MATHS LAB	Core (Departmental)	Hard	0	4	0	2
MAW508 MAW509 MAW231 MAW225 MAW119 CSW102	BASKET OF WORKSHOP ELECTIVES(ANY ONE)	Core (Departmental)	WORKSHOP	0	3	0	2
MAN634	PROJECT	Core (Departmental)	NTCC	0	0	6	6

- BASKET OF WORKSHOP ELECTIVES (ANY ONE):**
- 1) SCILAB —MAW508
  - 2) STATISTICS USING EXCEL —MAW119
  - 3) MATHEMATICA--MAW509
  - 4) SPSS —MAW231
  - 5) LATEX—MAW225
  - 6) HTML5 & CSS-CSW102

**DETAILED SYLLABUS  
FOURTH SEMESTER**

<b>Course Title/ Code</b>	<b>WAVELET ANALYSIS- MAH627-T</b>
<b>Course Type:</b>	Core (Departmental)
<b>Course Nature:</b>	Hard
<b>L-P-O Structure</b>	(4-0-0)
<b>Objective</b>	The student would be able to apply the concepts of theory of wavelets for solving problems in mathematics and signal processing.

	<b>Sections</b>	<b>Weightage</b>
<b>Syllabus</b>	A	25%
	B	25%
	C	25%
	D	25%
	<b>TOTAL</b>	<b>100%</b>

**Section A**

Study of Spaces  $l^2(\mathbf{z}_N)$ ,  $l^2(\mathbf{z})$ ,  $l^2[0, 2\pi)$ ,  $L^1(\mathbf{R})$  &  $L^2(\mathbf{R})$ , Discrete Fourier Transform, Properties of DFT, Inverse Discrete Fourier Transform, Convolution, The Fast Fourier Transform.

**Section B**

Construction of Wavelets on  $\mathbf{Z}_N$ : The first stage wavelets on  $\mathbf{Z}_N$ , Up-sampling operator, Down-sampling operator, The iteration step wavelets on  $\mathbf{Z}_N$ ,  $P^{th}$  stage wavelet basis, Examples & applications.

Wavelets on  $\mathbf{Z}$  :  $l^2(\mathbf{Z})$ , Complete orthonormal sets in Hilbert Space, Fourier Series, The Fourier transform and convolution on  $l^2(\mathbf{Z})$ , The first stage wavelets on  $\mathbf{Z}$ , The iteration steps for Wavelets on  $\mathbf{Z}$ , Examples.

**Section C**

Wavelets on  $\mathbf{R}$  :  $L^1(\mathbf{R})$  &  $L^2(\mathbf{R})$ , Fourier & Inverse Fourier Transform on  $\mathbf{R}$ , Properties of Fourier transform, Orthonormal Wavelets, Characterization of Orthonormal Wavelets, Some standard Wavelets (Haar Wavelets, Shannon Wavelets, Journe's Wavelets, Meyer Wavelets, Daubechies' family of wavelets in detail), Multiresolution Analysis, Father Wavelets & Mother Wavelets, Construction of Wavelets through MRA, Scaling function.

**Section D**

Characterization of Scaling function, Low-pass filter & High Pass filter, Characterizations of Low & High pass filter, Band limited Wavelets, Compactly Supported Wavelets, Minimally-Supported Frequency (MSF) Wavelets, Wavelet Sets, Characterization of MSF wavelets & Wavelet Sets, Dimension Functions, Characterization of MRA Wavelets, Wavelet Transform.

**Recommended Books:**

1. Michael W. Frazier, An Introduction to Wavelets through Linear Algebra, Springer
2. Hernandez & Weiss, A First Course of Wavelets, CRC Press
3. Charles K. Chui, An Introduction to Wavelets :
4. George Bachman, Lawrence Narici, Edward Beckenstein , Fourier and Wavelet Analysis,



<b>Course Title/ Code</b>	<b>FLUID MECHANICS- MAH628-T</b>
<b>Course Type</b>	Core (Departmental)
<b>Course Nature</b>	Hard
<b>L-P-O Structure</b>	4-0-0
<b>Objective</b>	The student would be able to apply the concepts of fluid mechanics for solving problems related to fluids.

	<b>Sections</b>	<b>Weightage</b>
<b>Syllabus</b>	A	25%
	B	25%
	C	25%
	D	25%
	<b>TOTAL</b>	<b>100%</b>

#### **Section A**

Physical Properties of fluids, Concept of fluids, Continuum Hypothesis, Density, Specific weight, Specific volume. Kinematics: Lagrangian and Eulerian methods, Steady and Unsteady flows, Uniform and Non uniform flows, Stream lines, Path lines and streak lines, Equation of continuity (Cartesian, polar & cylindrical coordinates), Equivalence of the two forms of Equation of continuity, velocity potential, Irrotational & Rotational flows, Boundary Surface, Conservation of Momentum: Euler's equation, Equation of motion of inviscid fluids, Bernoulli's equation, Lagrange's equation.

#### **Section B**

Viscous fluid flow: Stress analysis, Symmetry of stress tensor, stress in a fluid at rest and in motion, Transformation of stress components, Principal stresses and principal directions, Strain analysis, Rate of strain quadric, Navier Stokes equation of motion of viscous fluid, Equation of energy, Dissipation of energy, Vorticity and circulations & viscous fluids, Diffusion of vorticity, the equations of state, Reynolds number.

#### **Section C**

Conservation Laws : Equation of conservation of mass, equation of conservation of momentum, Navier Stokes equation, Equation of moments of momentum, Equation of energy, Basic equations in different co-ordinate systems, Boundary conditions.

#### **Section D**

Irrotational Motion:- General motion of a fluid element, Vorticity, Flow and Circulation, Stoke's theory, Kelvin's circulation theory Motion in two dimensions:- Stream function & its physical interpretation complex potential and complex velocity, Motion in two dimensions; Stream function, Complex potential, Source, Sink, Doublet, Complex potential and images with respect to straight line and circle, Milne-Circle theorem, Blasius theorem.

**Recommended Books:**

1. S.W.Yuan, Foundation to Fluid Mechanics.
2. F. Chorlton, Text book of Fluid Dynamics.
3. Bansi Lal, Theoretical Hydro-Dynamics.
4. M. Ray and Sharma, A text book of Fluid –Dynamics.
5. R. K. Gupta, Fluid Dyanamics

<b>Course Title/ Code</b>	<b>ALGEBRAIC TOPOLOGY- MAH629-T</b>
<b>Course Type:</b>	Elective (Departmental)
<b>Course Nature:</b>	Hard
<b>L-P-O Structure</b>	(4-0-0)
<b>Objective</b>	The student would be able to conceptualize and apply the concepts of Algebraic topology

	<b>Sections</b>	<b>Weightage</b>
<b>Syllabus</b>	A	25%
	B	25%
	C	25%
	D	25%
	<b>TOTAL</b>	<b>100%</b>

#### **Section A**

Introduction, Topological groups, Paths, Homotopies and the fundamental group, Categories and functors, Functorial properties of the fundamental group, Brouwer's theorem and its applications.

#### **Section B**

Homotopies of maps, Deformation retracts, Fundamental group of the circle, Covering projections, Lifting of paths and homotopies, Action of  $\Pi_1(X, x_0)$  on the fibers  $p^{-1}(x_0)$ , The lifting criterion.

#### **Section C**

Deck transformations, Orbit spaces, Fundamental groups of  $SO(3, \mathbb{R})$  and  $SO(4, \mathbb{R})$ , Coproducts and push-outs, Adjunction spaces, The Seifert Van Kampen theorem.

#### **Section D**

Homology theory, Singular complex of a topological space, The homology groups and their functoriality, Homotopy invariance of homology, Small simplicies, The Mayer Vietoris sequence, Abelianization of the fundamental group, The Mayer Vietoris sequence, Maps of spheres, Relative homology, Excision theorem, Inductive limits, Jordan Brouwer separation theorem.

#### **Recommended Books:**

1. Allen Hatcher, Algebraic Topology. Cambridge, UK: Cambridge University Press
2. William S. Massey, A Basic Course in Algebraic Topology. New York, NY: Springer-Verlag
3. Glen Bredon, Topology and Geometry
4. James R. Munkres, Topology (2nd Edition) Pearson Education Pve. Ltd., Delhi-2002

<b>Course Title/ Code</b>	<b>CRYPTOGRAPHY- MAH630-T</b>
<b>Course Type:</b>	Elective (Departmental)
<b>Course Nature:</b>	Hard
<b>L-P-O Structure</b>	(4-0-0)
<b>Objective</b>	The student would be able to conceptualize and apply the concepts of Cryptography.

	<b>Sections</b>	<b>Weightage</b>
<b>Syllabus</b>	A	25%
	B	25%
	C	25%
	D	25%
	<b>TOTAL</b>	<b>100%</b>

#### **Section A**

Secure communications, Shift ciphers, Affine ciphers, Vigenere cipher key, Symmetric key, Public key, Block ciphers, One-time pads, Secure random bit generator, Linear feedback shift register sequences.

#### **Section B**

Differential cryptanalysis, Modes of DES, Attack on DES, Advanced encryption standard.

#### **Section C**

RSA, Attacks on RSA, Diffie-Hellman key exchange, ElGamal public key cryptosystem, cryptographic hash function

#### **Section D**

RSA signatures, ElGamal signature, Hashing and signing, Digital signature algorithm.

#### **Recommended Books:**

1. Johannes A. Buchmann, Introduction to Cryptography, Springer 2000.
2. Douglas Robert Stinson, Cryptography - Theory and Practice, Chapman Hall / CRC 2006.
3. Wade Trappe and Lawrence C. Washington, Introduction to Cryptography with Coding Theory, Pearson Prentice Hall, 2006.

<b>Course Title/ Code</b>	<b>STRUCTURES ON A DIFFERENTIABLE MANIFOLD – MAH631-T</b>
<b>Course Type:</b>	Elective (Departmental)
<b>Course Nature:</b>	Hard
<b>L-P-O Structure</b>	(4-0-0)
<b>Objective</b>	The student would be able to conceptualize and apply the concepts of Differential manifold.

	<b>Sections</b>	<b>Weightage</b>
<b>Syllabus</b>	A	25%
	B	25%
	C	25%
	D	25%
	<b>TOTAL</b>	<b>100%</b>

#### **Section A**

Almost Complex Manifolds : Elementary notions, Nijenhuis tensor Eigen values of F, Integrability conditions, Contravariant and covariant analytic vectors, F-connection, Quaternion Structure

#### **Section B**

Almost Hermitian Manifolds: Definition, Almost analytic vector fields, Curvature tensor, Linear connections, Almost quaternion Metric structure.

#### **Section C**

Kaehler Manifolds: Definition. Curvature tensor, Affine connection, Properties of projective, Conformal, Concircular and conharmonic curvature tensors, Contravariant almost analytic vector, Quaternion Kaehler manifold.

#### **Section D**

Nearly Kaehler Manifolds: Introduction, Curvature identities, Almost analytic vectors.

#### **Recommended Books:**

1. R.S. Mishra: Structure on differentiable manifold and their application, ChandramaPrakashan, Allahabad, 1984.
2. K. Yano and M. Kon: Structures of Manifolds, World Scientific Publishing Co. Pvt. Ltd., 1984.

<b>Course Title/ Code</b>	<b>THEORY OF ELASTICITY &amp; FRACTURE MECHANICS- MAH632-T</b>
<b>Course Type:</b>	Elective (Departmental)
<b>Course Nature:</b>	Hard
<b>L-P-O Structure</b>	(4-0-0)
<b>Objective</b>	The student would be able to apply the concepts of fracture mechanics to avoid fracture in a body.

	<b>Sections</b>	<b>Weightage</b>
<b>Syllabus</b>	A	25%
	B	25%
	C	25%
	D	25%
	<b>TOTAL</b>	<b>100%</b>

#### **Section A**

Analysis of stress and strain, Equilibrium equations , Compatibility equations, stress strain relationship, Generalized Hooke's law, Stress, Strain & Elasticity, Stiffness, Strength and Toughness, Types of mechanical behavior, Relevance, Measurement, Data, Macroscopic, Continuum behavior, Physical mechanisms controlling behavior, Introduction, Stress, Strain, Compliance and stiffness tensors, Physical origin of elastic moduli, Generalized Hooke's law and its application to crystals, Designing for modulus and Composites.

#### **Section B**

Plane stress and plane strain, Simple two dimensional problems in Cartesian and polar co-ordinates.

#### **Section C**

Importance of Fracture Mechanics, Griffith Fracture Theory, Crack Driving Force & Energy Release Rate, Modes of fracture, Stress intensity factors, Similitude, Role of Crack-tip Plasticity-Plastic Zone Size & Shape, K-dominance, Fracture Toughness-Microstructural issues. Significance of fracture mechanics, Griffith energy balance approach, Irwin's modification to the Griffith theory, Stress intensity approach, Crack tip plasticity, Fracture toughness, sub-critical crack growth, Influence of material behaviour, I, II & III modes, Mixed mode problems.

#### **Section D**

Fatigue Crack Growth: Description of fatigue crack growth using stress intensity factor, Effects of stress ratio and crack tip plasticity – crack closure, Prediction of fatigue crack growth under constant amplitude and variable amplitude loading, Fatigue crack growth from notches – the short crack problem. Practical Problems:- Through cracks emanating from holes, Corner cracks at holes, Cracks approaching holes, fracture toughness of weldments, Service failure analysis, applications in pressure vessels, pipelines and stiffened sheet structures.

**Recommended Books:**

1. Ewalds, H.L. & Wanhill, R.J.H., Fracture Mechanics – Edward Arnold Edition
2. Timoshenko, S. and Goodier J.N. "Theory of Elasticity", McGraw Hill Book Co., Newyork, 1988.
3. Broek, D. Elementary Engineering Fracture Mechanics, Sijthoff & Noordhoff Int. Pub., 1988.
4. Broek, D. The Practical Use of Fracture Mechanics, Kluwer Academic Pub., 1990.
5. Hellan, D. Introduction to Fracture Mechanics, McGraw Hill Book Company, 1985.
6. Kumar, P. Elements of Fracture Mechanics, Wheeler Publishing, 1998.

<b>Course Title/ Code</b>	<b>MATHS LAB- MAH633-P</b>
<b>Course Type:</b>	Core (Departmental)
<b>Course Nature:</b>	Hard
<b>L-P-O Structure</b>	(0-4-0)
<b>Objective</b>	The student would be able to apply the tools of Matlab software for solving the problems of Fourier & Wavelet Analysis.

### LAB EXERCISE:

1. To evaluate discrete Fourier transform (DFT) of functions or signals using MATLAB.
2. To evaluate inverse discrete Fourier transform (IDFT) of functions or signals using MATLAB.
3. To evaluate Fast Fourier transform (FFT) of functions or signals using MATLAB.
4. To evaluate Inverse Fourier transform (IFFT) of functions or signals using MATLAB.
5. Evaluation of Fourier basis using MATLAB.
6. To plot discrete and continuous signals.
7. To evaluate translation of a given signals and plot the translated signals.
8. To plot discrete Fourier transform () of a given signal(z) and also plot real & imaginary part of (), phase(angle) and magnitude of ().
9. To find convolution of a given signals using MATLAB.
10. To evaluate first stage Shannon basis using MATLAB and plot the same.
11. To evaluate first stage real Shannon basis using MATLAB and plot the same.
12. To evaluate first-stage Haar basis using MATLAB and plot the same.